

$$\min_X ||u - \mathcal{A}(X)||_2^2 + \lambda ||X||_* = \min_{U,V} ||u - \mathcal{A}(UV^*)||_2^2 + \frac{\lambda}{2} (||U||_F^2 + ||V||_F^2)$$