

$$\mathcal{O}\left(\exp(1.9(\log N)^{1/3}(\log \log N)^{2/3})\right)$$